



Power of a Power

Video Notes

[Video Link](#)

Power of a Power

Background Knowledge:

- Multiplying Monomials

Simplify:

$$(2^5)^3 \rightarrow \underbrace{2^5 \cdot 2^5 \cdot 2^5}_{\substack{\text{2} \cdot \text{2} \cdot \text{2} \cdot \text{2} \cdot \text{2} \\ \text{2} \cdot \text{2} \cdot \text{2} \cdot \text{2} \cdot \text{2} \\ \text{2} \cdot \text{2} \cdot \text{2} \cdot \text{2} \cdot \text{2}}} = 2^{15} \rightarrow 5 \cdot 3$$

2^5 raised to the power of 3
(multiplied by itself 3 times)

* rule for multiplication:
add exponents with
like bases

$$5 + 5 + 5 = 15$$

$$(2^5)^{100}$$

Simplify:

$$(x^2)^6 \rightarrow \underbrace{x^2 \cdot x^2 \cdot x^2 \cdot x^2 \cdot x^2 \cdot x^2}_{x^2 \text{ multiplied by itself 6 times (power of 6)}} = x^{12} \rightarrow 2 \cdot 6$$

x^2 multiplied by itself 6 times (power of 6)

Simplify:

$$(a^2bc^5)^3 \rightarrow \underbrace{a^2bc^5 \cdot a^2bc^5 \cdot a^2bc^5}_{\substack{2 \cdot 3 \\ 1 \cdot 3 \\ 5 \cdot 3}} = a^6b^3c^{15}$$

a^2bc^5 multiplied by itself 3 times (power of 3)

Simplify: $(2y^7)^6$

coefficient (not an exponent)

$$2y^7 \cdot 2y^7 \cdot 2y^7 \cdot 2y^7 \cdot 2y^7 \cdot 2y^7 = 64y^{42}$$

2^6 (pointing to 64) and $7 \cdot 6$ (pointing to 42)

$2y^7$ multiplied by itself 6 times (power of 6)

Common mistakes:

- $7 + 6$
 → No! we are raising a power to a power (multiply exponents), not multiplying bases (add exponents)
 $(y^7)^6 = y^{42}$ vs. $y^7 \cdot y^6 = y^{13}$
- coefficient is $2 \cdot 6$
 → No! 2 is also being raised to the power of 6.

You try!

$$(5x^8)^3 = 125x^{24}$$

$$5x^8 \cdot 5x^8 \cdot 5x^8$$

$$= 125x^{24}$$

$5^3 = 125$ (pointing to 125)

$8 \cdot 3 = 24$ (pointing to 24)

Conclusion:

- To raise a power to a power, we multiply the exponents
- If an expression being raised to a power has a coefficient, make sure to raise that coefficient to the power as well.